ISSN 2310-6697

otoiser—open transactions on independent scientific-engineering research

FUNKTECHNIKPLUS # JOURNAL

Théorie—Expérimentation—Métrologie—Logiciel—Applications

ISSUE 11 - FRIDAY 30 SEPTEMBER 2016 - YEAR 4

1 Contents

2 About

3 Editorial Board — Technical Support

4 Information for Peers - Guiding Principles

Telecommunications Engineering - Métrologie

7 Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 4: Non-Zero Length Through in Full Two-Port SLOT Calibration N.I. Yannopoulou, P.E. Zimourtopoulos



This small European Journal is In the Defense of Honesty in Science and Ethics in Engineering

Publisher — otoiser—open transactions on independent scientific engineering research, www.otoiser.org — info@otoiser.org : Hauptstraße 52, 2831 Scheiblingkirchen, Austria

Language — We emphasize the origins of the Journal by using English, German and French, as well as, a Hellenic vignette in the cover page. However, since we recognize the dominance of US English in the technical literature, we adopted it as the Journal's language, although it is not our native language.

Focus — We consider Radio—FUNK, which still creates a vivid impression of the untouchable, and its Technology—TECHNIK, from an Advanced—PLUS point of view, Plus—PLUS Telecommunications Engineering, Electrical Engineering and Computer Science, that is, we dynamically focus at any related scientific-engineering research regarding Théorie, Expérimentation, Métrologie, Logiciel, ou Applications.

Scope — We emphasize this scope broadness by extending the title of the Journal with a Doppelkreuz-Zeichen # which we use as a placeholder for substitution of our Editorial Team disciplines: # Telecommunications etc. as above, or # High Voltage, # Software Engineering, # Simulation etc. as below.

Frequency – We publish 3 issues per year: on 31st of January, on 31st of May, and on 30th of September, as well as, an extra issue every 3 papers and a volume every 2 years.

Editions — We increase the edition number of an issue only when is needed to reform one or more of its papers—thus to increase their version numbers—but we keep unchanged its 1st edition date shown on its front page and we number its pages sequentially from 1. We count the editions of *About* separately.

Format — We use a fixed-space font, hyphenation, justification, unfixed word spacing, and the uncommon for Journals **A5** (half A4) page size to achieve WYSIWYG printing and clear reading of 2 to 4 side-by-side pages on wide-screen displays.

Printing-on-Demand — We can email gratis PDF files at 300-4000 dpi in booklet page scaling of brochure and book type.

Copyright — We publish under a Creative Commons Attribution, CC-BY 3.0 Unported or CC-BY 4.0 International, License only.

Please download the latest About edition from
 http://about.ftpj.otoiser.org

<u>Editorial Team</u>

Electrical Engineering

Professor Michael Danikas, mdanikas@ee.duth.gr EECE, Democritus University of Thrace, Greece # High Voltage Engineering # Insulating Materials

Assistant Professor Athanasios Karlis, akarlis@ee.duth.gr EECE, Democritus University of Thrace, Greece

Electrical Machines # Renewable Energies # Electric Vehicles

Computer Science

Professor Vasilis Katos, vkatos@bournemouth.ac.uk
Head of Computer and Informatics Dept, Bournemouth Univ, UK
Computer Engineering # Software Engineering # Cyber Security

Lecturer Sotirios Kontogiannis, skontog@gmail.com Business Administration Dept, TEI, Western Macedonia, Greece # Internet Engineering # Learning Management Systems

Dr. Apostolos Syropoulos, asyropoulos@yahoo.com BSc-Physics, MSc-Computer Science, PhD-Computer Science Independent Researcher, Xanthi, Greece

Hypercomputation # Fuzzy Computation # Digital Typography

Telecommunications Engineering

Dr. Nikolaos Berketis, nberketis@gmail.com BSc-Mathematics, MSc-Applied Maths, PhD-Applied Mathematics Independent Researcher, Athens, Greece

Applied EM Electromagnetics # Applied Mathematics

Dr. Nikolitsa Yannopoulou, yin@arg.op4.eu [*] Diploma Eng-EE, MEng-Telecom-EECE, PhD-Eng-Antennas-EECE Independent Researcher, Scheiblingkirchen, Austria

Dr. Petros Zimourtopoulos, pez@arg.op4.eu [*] BSc-Physics, MSc-Radio-Electronics, PhD-Antennas-EE Independent Researcher, Scheiblingkirchen, Austria

- # Antennas # Metrology # EM Software # Simulation # Virtual Labs
- # Applied EM # Education # FLOSS # Amateur Radio # Electronics
- * Copy and Layout Editing, Proof Reading, Issue and Website Management, Paper and About Reprints, Volumes and Web Pages

Technical Support

Konstantinos Kondylis, kkondylis@gmail.com Diploma Eng-EECE, MEng-Telecom-EECE, Doha, Qatar Christos Koutsos, ckoutsos@gmail.com Diploma Eng-EECE, MEng-Telecom-EECE,Bratislava,SK This is a small, but independent, low profile Journal, in which we are all—Authors, Reviewers, Readers, and Editors free at last to be Peers in Knowledge, without suffering from Journal roles or positions, Professional—Amateur—Academic statuses, or established "impact factorizations", under the following guiding principles:

Authors — We know what Work means, we respect the Work of the Independent Researcher in Science and Engineering and we want to exhibit his Work. Thus, we decided to found this Free and Open Access Journal in which to publish this Work. Furthermore, as we care indeed for the Work of the technical author—especially a young or a beginner one—we strongly support the publication of his Work, as follows:

- 1 We do not demand from the author to transfer his own copyright to us. Instead, we only consider papers resulting from original research work only, and only if the author can assure us that he owns the copyright of his own paper as well as that he submits to the Journal either an original copy or a revised version of his own paper, for possible publication after review—or even for immediate republication, if this paper has already been published after review—but, in any case under a Creative Commons Attribution, CC-BY 3 Unported or CC-BY 4 International, License, only.
- 2 We encourage the author to submit his own paper written just in Basic English plus Technical Terminology.
- 3 We encourage the author even to select a pen name, which may drop it at any time to reveal his identity.
- 4 We encourage the author to submit an accepted for publication paper, which he was forced to decline that publication because it would be based on a review with unacceptable evaluation or derogatory comments.
- 5 We encourage the author to submit any paper that was rejected after a poor, impotent, inadequate, unreasonable, irresponsible, incompetent, or "just ticking" review.
- 6 We encourage the author to submit an unreviewed paper of his own that he uploaded on some Open Access repository.
- 7 We encourage the author to upload his published paper in our Journal to at least one Truly Free Open Repository, e.g. such as http://viXra.org and https://archive.org.

- 8 We provide the author with the ability to update, at any time, the reference links of his paper.
- 9 We provide the author with a decent, express, peer review process, of up to just 4 weeks, by at least 2, either anonymous or onymous, reviewers.
- 10 We provide the author with the option to choose from 2 review processes: the traditional, anonymous, close one, as well as, a contemporary, onymous, open review in our private mailing list for Peer Discussion.
- 11 Under the Clause 1 : We immediately accept for publication a research paper directly resulting from a Project Report, or a Diploma-, Master-, or PhD-thesis, which already the author has successfully defended before a committee of experts, as long as he can mention 2 members of this committee who approved his Work.
- 12 Under the Clause 1 : We immediately accept for publication any paper which is not Openly Accessible on the Internet.
- 13 We immediately publish online a paper, as soon as it is accepted for publication in the Journal.
- 14 We quickly publish an extra issue—that is in excess of the 3 issues we publish a year—as soon as the review process of 3 papers is completed.

Reviewers — Every peer may voluntarily become a reviewer of the Journal in his skillfulness for as long as he wishes. In addition, each author of the Journal must review one paper in his expertness for each one of his published papers.

Readers — Every reader is a potential post-reviewer: we welcome comments and post-reviews in our private mailing list for Peer Discussion.

Editors — Every editor owns a PhD degree—to objectively prove that he really has the working experience of passing through the dominant publishing system. An editor pre-reviews a paper in order to check its compliance to our guiding principles and to select the appropriate reviewers of it. We can accept for consideration papers only in the expertise areas currently shown in the Editorial Team page, above. However, since we are very willing to amplify and extend the Scope of the Journal, we welcome the volunteer expert, in any related subject, who wants to join the Editorial Team as long as he unreservedly accepts our guiding principles.

About

Electronic Publishing

We regularly use the Free Libre Open Source Software Libre Office with the Free Liberation Mono font and the Freewares PDFCreator and PDF-Xchange Viewer. We also use, with some basic html code of ours: the Free Open Source Software Open Journal System OJS by the Public Knowledge Project PKP installed in our website, and the Free Open Digital Library of Internet Archive website, where we upload the FTP#J Collection of Issues, Paper reprints, *About* documents, and Volumes, in both portrait and landscape orientations, for download or very clear online reading with the Free Open Source BookReader.

Submissions

We can only consider papers written in the preferable and recommended odt format of LibreOffice, or even a paper in the MS Office with MathType doc format, if it would be proved that it is fully compatible with LibreOffice indeed.

Legal Notice – It is taken for granted that the submitter– correspondent author accepts, without any reservation, the totality of our publication conditions as they are analytically detailed here, in this *About*, as well as, that he also carries, in the case of a paper by multiple authors, the independent will of each one of his co-authors to unreservedly accept all the aforementioned conditions for their paper.

Internet Addresses

Submissions : sub@ftpj.otoiser.org
Send Updates : updates@ftpj.otoiser.org
Printing-on-Demand : pod@ftpj.otoiser.org
Technical Support TS : technical-support@ftpj.otoiser.org
Principal Contact : principal-contact@ftpj.otoiser.org

Peer Discussion List : www.peers.ftpj.otoiser.org
Editorial Team & TS List : www.etts.ftpj.otoiser.org

The FTP#J Collection at Internet Archive Digital Library : https://archive.org/details/@funktechnikplusjournal

Sample Paper Templates : www.template.ftpj.otoiser.org
Reference Link Updates : www.updates.ftpj.otoiser.org
Internet Publishing : www.ftpj.otoiser.org

This document is licensed under a Creative Commons Attribution 4.0 International License – <u>https://creativecommons.org/licenses/by/4.0</u>

Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 4: Non-Zero Length Through in Full Two-Port SLOT Calibration

N.I. Yannopoulou, P.E. Zimourtopoulos *

Antennas Research Group, Austria

Abstract

The most accurate full two-port calibration of a VNA Vector Network Analyzer requires a Direct or Zero-Length Through connection. However, it is not uncommon at all to have one or two cables and a DUT Device Under Test with incompatible connectors, either of different type or of the same type/sex, which enforce then the use of some kind of barrel or adapter. Thus, in this paper, we study these cases of Indirect or Non-Zero Length Through, we estimate the effects of such connections on the measurement uncertainty by using our theory of Differential Error Regions and Intervals DERs/DEIs, and we evaluate our resulting method by applying it in practice to a built two-port network, which was measured against frequency with a SLOT calibrated VNA extended by two lengthy cables.

Keywords

microwave measurements, network analyzer, differential error region, differential error interval, calibration

Introduction

A full two-port calibration for the measurement of a two port DUT (Device Under Test) or AUT (Antenna Under Test) with a Vector Network Analyzer involves the wellknown two-port error model shown in Fig. 1, for both the forward and reverse directions. The notation of one symbol per system error was adopted in order to keep the rather lengthy expressions as simple as possible. So, D is the Directivity error E_D , M the Source Match error E_M or E_S , R the frequency Response error E_R , L the Load Match error E_L , T the transmission Tracking error E_T , X the isolation or Crosstalk error E_Y , with the primed symbols for the reverse direction and m_{ij} the measurements of the DUT. Thus, 12 System Errors and 4 unknowns, the S-parameters of the DUT or AUT must be determined. In [1], [2] the most accurate case of a Direct Zero-Length through, often referenced as "Thru", was examined and presented in detail.

However, there are at least two cases where a Zero-Length Through is impossible and a Non-Zero Length Through is inevitable. First, when the DUT or the cables has the same connectors on each port both in type and sex, and second, when its ports have different type of connector. The Through Standard can be represented then, in general, by the two-port flow graph shown at Fig. 2, where the symbols T_{ii} were used for its S-parameters.

The first announcement of the present work was a twenty minute presentation in the 32nd ANAMET meeting of the National Physical Laboratory (NPL) in 16 October 2009 in Teddington, which is available either in

"http://resource.npl.co.uk/do cs/networks/anamet/members_on ly/meetings/32/20091016_aname t32_thrace.pdf"

or from

www.antennas.gr/anamet/32/

Research

The typical differential errors dS_{11} and dS_{21} of the S_{11} and S_{21} parameters are given by (1) and (2) respectively [1] where (3) is their common denominator P. The expressions are general, and are simplified a lot when the SLO calibration standards are considered. What it is really changed with the Indirect Through connection between the two ports is the L and T system errors shown with blue color and their differential errors dL and dT shown with red color, for the forward and the reverse direction.

The full expressions of these quantities are given in (4)-(8) where the red characters in L, T expressions indicate what is added when the case of the Non-Zero Length Through is considered in comparison with the Direct Through case represented by black characters. At the dL, dT expressions four (4) more terms occur which are depended on the differential errors dT_{ii} of the Through standard. These relations result from the equivalent svstem of Fig. 1 when the DUT is substituted with the Through represented by the known two port of Fig. 2 and m_{ij} with the corresponding tij measurements.

FUNKTECHNIKPLUS # JOURNAL



Fig. 1: Two-Port Error Model: Forward and Reverse direction

$$\begin{split} dS_{11} &= \{T T'(1 - MS_{11})[R' + M'(m_{22} - D')](dm_{11} - dD) \\ &- RR'L(1 - L'S_{11})[(m_{21} - X)(dm_{12} - dX') + (m_{12} - X')(dm_{21} - dX)] \\ &+ M'T T'[(m_{11} - D)(1 - MS_{11}) - RS_{11}](dm_{22} - dD') \\ &- T T'S_{11}(m_{11} - D)[R' + M'(m_{22} - D')]dM \\ &+ T T'(m_{22} - D')[(m_{11} - D)(1 - MS_{11}) - RS_{11}]dM' \\ &- (R'L(1 - L'S_{11})(m_{12} - X')(m_{21} - X) \\ &+ T T'S_{11}[R' + M'(m_{22} - D')])dR \\ &- (RL(1 - L'S_{11})(m_{12} - X')(m_{21} - X) \\ &- T T'[(m_{11} - D)(1 - MS_{11}) - RS_{11}])dR' \\ &- RR'(m_{12} - X')(m_{21} - X)[(1 - L'S_{11})dL - LS_{11}dL'] \\ &+ [(m_{11} - D)(1 - MS_{11}) - RS_{11}][R' + M'(m_{22} - D')] \\ &\cdot (T'dT + TdT')\}/P \end{split}$$

$$dS_{21} = \{-MTT'S_{21}[R'+M'(m_{22} - D')](dm_{11} - dD) + RR'LL'S_{21}(m_{21} - X)(dm_{12} - dX')$$

$$+ R\{T'[R' + (m_{22} - D')(M' - L)] + R'LL'S_{21}(m_{12} - X')\}(dm_{21} - dX) + T'(R(m_{21} - X)(M' - L) - M'TS_{21}[R + M(m_{11} - D)])(dm_{22} - dD') - TT'S_{21}(m_{11} - D)[R' + M'(m_{22} - D')]dM + T'(m_{22} - D')(R(m_{21} - X) - TS_{21}[R + M(m_{11} - D)])dM' + {(m_{21} - X)(T'(m_{22} - D')(M' - L) + R'[T' + LL'S_{21}(m_{12} - X')]) - TT'S_{21}[R' + M'(m_{22} - D')]\}dR + (R(m_{21} - X)[T' + LL'S_{21}(m_{12} - X')] - TT'S_{21}[R + M(m_{11} - D)])dR' + R(m_{21} - X)[R'L'S_{21}(m_{12} - X') - T'(m_{22} - D')]dL + RR'LS_{21}(m_{12} - X')(m_{21} - X)dL' - T'S_{21}[R + M(m_{11} - D)][R' + M'(m_{22} - D')]dT + (R(m_{21} - X)[R' + (m_{22} - D')(M' - L)] - TS_{21}[R + M(m_{11} - D)][R' + M'(m_{22} - D')]]dT'\}/P (2)$$

$$P = T T'[R' + M'(m_{22} - D')][R + M(m_{11} - D)] - RR'LL'(m_{12} - X')(m_{21} - X)$$
(3)

$$L = \{T_{11}[R + M(t_{11} - D)] - (t_{11} - D)\} / \{[R + M(t_{11} - D)]\Delta - (t_{11} - D)T_{22}\}$$
(4)

$$T = -T_{12}(t_{21} - X)R / \{ [R + M(t_{11} - D)]\Delta - (t_{11} - D)T_{22} \}$$
(5)

$$dL = \{ [(1 - MT_{11}) + L(M\Delta - T_{22})(dD - dt_{11}) + (t_{11} - D)(T_{11} - L\Delta)dM + (T_{11} + L\Delta)dR + [R + M(t_{11} - D)](1 - LT_{22})dT_{11} + L\{(t_{11} - D) - T_{11}[R + M(t_{11} - D)]\}dT_{22} + L[R + M(t_{11} - D)](T_{21}dT_{12} + T_{12}dT_{21})\} / \{ [R + M(t_{11} - D)]\Delta - (t_{11} - D)T_{22} \}$$
(6)

$$dT = \{T(M\Delta - T_{22})(dD - dt_{11}) - T\Delta(t_{11} - D)dM - [T\Delta + (t_{21} - X)T_{12}]dR + T[R + M(t_{11} - D)](T_{12}dT_{21} - T_{22}dT_{11}) - \{R(t_{21} - X) - T[R + M(t_{11} - D)]T_{21}\}dT_{12} - T\{T_{11}[R + M(t_{11} - D)] - (t_{11} - D)\}dT_{22} - RT_{12}(dt_{21} - dX)\} / \{[R + M(t_{11} - D)]\Delta - (t_{11} - D)T_{22}\}$$
(7)

 $\Delta \equiv T_{11}T_{22} - T_{12}T_{21}$ (8)

expressions of L, T, dL, dT

and the corresponding primed ones L', T', dL', dT' for the reverse direction, as func-

tions of the differentials for standard uncertainties dA,

dB, dC, dT_{ij} and for their

measurement inaccuracies da,

db, dc, dt_{ij} of all the loads

used for the full two-port calibration we take the

rather lengthy expressions,



Fig. 2: Non-Zero Length Through

Following the same procedure as in [1], for the final

$$L = (ab + ct_{11})(B - A)(T_{11} - C) + (bc + at_{11})(C - B)(T_{11} - A) + (ca + bt_{11})(A - C)(T_{11} - B) = [\Sigma (ab + ct_{11})(B - A)(T_{11} - C)]/G$$
(9)

$$T = -(t_{21} - X)T_{12}(A - B)(a - b)(B - C)(b - c)(C - A)(c - a)]/GF$$

= -(t_{21} - X)T_{12}[[(A - B)(a - b)]/(GF) (10)

$$\begin{split} d\mathsf{L} &= \{\mathsf{T}_{12}\mathsf{T}_{21}\sum(\mathsf{B}-\mathsf{C})(\mathsf{b}-\mathsf{t}_{11})(\mathsf{c}-\mathsf{t}_{11})[(\mathsf{B}-\mathsf{C})(\mathsf{b}-\mathsf{a})(\mathsf{c}-\mathsf{a})\mathsf{d}\mathsf{A} \\ &- (\mathsf{b}-\mathsf{c})(\mathsf{B}-\mathsf{A})(\mathsf{C}-\mathsf{A})\mathsf{d}\mathsf{a}] + \mathsf{T}_{12}\mathsf{T}_{21}[\prod(\mathsf{A}-\mathsf{B})(\mathsf{a}-\mathsf{b})] \, \mathsf{d}\mathsf{t}_{11} \\ &- \mathsf{T}_{12}\mathsf{T}_{21}\mathsf{E}^2\mathsf{d}\mathsf{T}_{11} - \mathsf{H}^2\mathsf{d}\mathsf{T}_{22} + \mathsf{E}\mathsf{H}(\mathsf{T}_{21}\mathsf{d}\mathsf{T}_{12} + \mathsf{T}_{12}\mathsf{d}\mathsf{T}_{21})\}/\mathsf{G}^2 \\ &= (1/\mathsf{G}^2)\{\mathsf{T}_{12}\mathsf{T}_{21}((\mathsf{B}-\mathsf{C})(\mathsf{b}-\mathsf{t}_{11})(\mathsf{c}-\mathsf{t}_{11}) \\ &\cdot [(\mathsf{B}-\mathsf{C})(\mathsf{b}-\mathsf{a})(\mathsf{c}-\mathsf{a})\mathsf{d}\mathsf{A} - (\mathsf{b}-\mathsf{c})(\mathsf{B}-\mathsf{A})(\mathsf{C}-\mathsf{A})\mathsf{d}\mathsf{a}] \\ &+ (\mathsf{C}-\mathsf{A})(\mathsf{c}-\mathsf{t}_{11})(\mathsf{a}-\mathsf{t}_{11}) \\ &\cdot [(\mathsf{C}-\mathsf{A})(\mathsf{c}-\mathsf{b})(\mathsf{a}-\mathsf{b})\mathsf{d}\mathsf{B} - (\mathsf{c}-\mathsf{a})(\mathsf{C}-\mathsf{B})(\mathsf{A}-\mathsf{B})\mathsf{d}\mathsf{b}] \\ &+ (\mathsf{A}-\mathsf{B})(\mathsf{a}-\mathsf{t}_{11})(\mathsf{b}-\mathsf{t}_{11}) \\ &\cdot [(\mathsf{A}-\mathsf{B})(\mathsf{a}-\mathsf{c})(\mathsf{b}-\mathsf{c})\mathsf{d}\mathsf{C} - (\mathsf{a}-\mathsf{b})(\mathsf{A}-\mathsf{C})(\mathsf{B}-\mathsf{C})\mathsf{d}\mathsf{c}]) \\ &+ \mathsf{T}_{12}\mathsf{T}_{21}[(\mathsf{A}-\mathsf{B})(\mathsf{a}-\mathsf{b})(\mathsf{B}-\mathsf{C})(\mathsf{b}-\mathsf{c})(\mathsf{C}-\mathsf{A})(\mathsf{c}-\mathsf{a})] \, \mathsf{d}\mathsf{t}_{11} \\ &- \mathsf{T}_{12}\mathsf{T}_{21}\mathsf{E}^2\mathsf{d}\mathsf{T}_{11} - \mathsf{H}^2\mathsf{d}\mathsf{T}_{22} + \mathsf{E}\mathsf{H}(\mathsf{T}_{21}\mathsf{d}\mathsf{T}_{12} + \mathsf{T}_{12}\mathsf{d}\mathsf{T}_{21})\} \end{split}$$

$$dT = \{(t_{21} - X)T_{12}\sum \{(A - B)(C - A)(a - b)(c - a)(T_{22}BC(b - c) + \Delta[B(t_{11} - b) - C(t_{11} - c)]) - G[F + 2(a - b)B(A - C)]\} + \{[\prod (a - b)](B - C)^2 dA - [\prod (A - B)](b - c)^2 da\}/(F^2G^2)\}$$

$$+ [\Pi (A - B)(a - b)] \{ (t_{21} - X) [T_{12}(Idt_{11} + E(T_{22}dT_{11} - T_{12}dT_{21}) + HdT_{22}) + HT_{22}dT_{12}]/6 + T_{12}(dX - dt_{21}) \}/(FG)$$

$$= \{ (t_{21} - X)T_{12}\{(A - B)(C - A)(a - b)(C - a)(T_{22}BC(b - c) + \Delta[B(t_{11} - b) - C(t_{11} - c)]) - G[F + 2(a - b)B(A - C)] \}$$

$$\cdot \{ (a - b)(b - c)(c - a)(B - C)^{2}dA$$

$$- (A - B)(B - C)(C - A)(b - c)^{2}da \}$$

$$+ \{ (B - C)(A - B)(b - c)(a - b)(T_{22}CA(c - a) + \Delta[C(t_{11} - c) - A(t_{11} - a)]) - G[F + 2(b - c)C(B - A)] \}$$

$$\cdot \{ (a - b)(b - c)(c - a)(C - A)^{2}dB$$

$$- (A - B)(B - C)(C - A)(c - a)^{2}db \}$$

$$+ \{ (C - A)(B - C)(c - a)(b - c)(T_{22}AB(a - b) + \Delta[A(t_{11} - a) - B(t_{11} - b)]) - G[F + 2(c - a)A(C - B)] \}$$

$$\cdot \{ (a - b)(b - c)(c - a)(A - B)^{2}dC$$

$$- (A - B)(B - C)(C - A)(a - b)^{2}dc \} / (F^{2}G^{2})$$

$$+ [(A - B)(a - b)(B - C)(b - c)(C - A)(c - a)]$$

$$\cdot \{ (t_{21} - X)[T_{12}(Idt_{11} + E(T_{22}dT_{11} - T_{12}dT_{21}) + HdT_{22}) + HT_{22}dT_{12}]/6$$

$$+ T_{12}(dX - dt_{21}) \}/(FG)$$

$$(12)$$

with

$$E = (ab + ct_{11})(B - A) + (bc + at_{11})(C - B) + (ca + bt_{11})(A - C)$$

= $\sum (ab + ct_{11})(B - A)$ (13)

$$F = cC(B - A) + aA(C - B) + bB(A - C) = \sum cC(B - A)$$
(14)

$$G = (\Delta - T_{22}C)(ab + ct_{11})(B - A) + (\Delta - T_{22}A)(bc + at_{11})(C - B) + (\Delta - T_{22}B)(ca + bt_{11})(A - C) = \sum (\Delta - T_{22}C)(ab + ct_{11})(B - A)$$
(15)

$$H = (ab + ct_{11})(B - A)(T_{11} - C) + (bc + at_{11})(C - B)(T_{11} - A) + (ca + bt_{11})(A - C)(T_{11} - B) = \sum (ab + ct_{11})(B - A)(T_{11} - C)$$
(16)

$$I = (\Delta - T_{22}C)c(B - A) + (\Delta - T_{22}A)a(C - B) + (\Delta - T_{22}B)b(A - C)$$

= $\sum (\Delta - T_{22}C)c(B - A)$ (17)

where
$$\sum$$
 and \prod produce, obviously from the above relations, two more terms, from the given one, by cyclic rotation of the letters a, b, c and A, B, C respectively. The corresponding L', T', dL', dT' for the reverse direction resulted from (9), (17) respectively by similar expressions, with the replacement of a, b, c and A, B, C with the primed ones and the subscripts 11, 12, 21 and 22 with 22, 21, 12 and 11 respectively, in all of their occurrences in t_{ij} or T_{ij}. The expressions (4)-(17) were mechanically cross verified using a developed software program for symbolic computations.

Tab. 1 contains the comparison between a SLOdT full two-port calibration when a Direct/Zero Length Through is possible and a SLOT full twoport calibration when a Non-Zero Length Through is inevitable. The number of measurements and their inaccuracies remains the same in both schemes as well as the number of standards and their uncer-

$$L = (t_{11} - D) / \{T_{12}T_{21}[R + M(t_{11} - D)]\}$$
(18)

$$T = (t_{21} - X)R / \{T_{21}[R + M(t_{11} - D)]\}$$
(19)

$$dL = - \{ [(1 - T_{12}T_{21}LM)(dD - dt_{11}) + T_{12}T_{21}(t_{11} - D)dM + T_{12}T_{21}LdR + [R + M(t_{11} - D)]dT_{11} + L(t_{11} - D)dT_{22} + L[R + M(t_{11} - D)] + (T_{21}dT_{12} + T_{12}dT_{21}) \} / \{ T_{12}T_{21}[R + M(t_{11} - D)] \}$$
(20)

$$dT = \{T_{12}T_{21}TM(dD - dt_{11}) - T_{12}T_{21}T(t_{11} - D)dM + [(t_{21} - X)T_{12} - T_{12}T_{21}T]dR - T[R + M(t_{11} - D)]T_{12}dT_{21} - \{R(t_{21} - X) - T[R + M(t_{11} - D)]T_{21}\}dT_{12} - T(t_{11} - D)dT_{22} + RT_{12}(dt_{21} - dX)\}/\{T_{12}T_{21}[R + M(t_{11} - D)]\}$$
(21)

Tab. 1: Full Two-Port Calibration

	Zero-Length Through	Non-Zero Length Through			
16	Measurements	\Rightarrow 16 Inaccuracies			
6	Standard Loads	\Rightarrow 6 Uncertainties			
		1 Through Load \Rightarrow 4 Uncertainties			
22	Complex Variables	26			
22	Complex Differential Errors	26			
44	Real Parameters	52			
44	Real Differential Errors	52			
S-DER SLOdT		S-DER SLOT			
20	Orthogonals + 2 Circles	22 Orthogonals + 4 Circles			
D	ER Contour: 160 Vertices	DER Contour: 176 Vertices			

It is important to be noted that if the simplified expressions (18) and (19) were used, then the two terms with the uncertainty in T_{11} and T_{22} parameters in L, and the two terms with the uncertainty in T_{12} and T_{22} parameters in T, shown in red color above, would be lost. Since, usually, the terms ii correspond to return loss, or SWR, at specifications, this loss would lead to an unreal reduction of the final uncertainty of the L, T system errors.

The corresponding final expressions are given by

$$L = [\sum (ab + ct_{11})(B - A)C] / (T_{12}T_{21}E)$$
(22)

FUNKTECHNIKPLUS # JOURNAL v1–14

v1–13 FUNKTECHNIKPLUS # JOURNAL

tainties for the corresponding one port (forward and reverse direction) calibration but one more two-port load is added, the Through, which introduces four (4) more uncertainties. Therefore, each Sparameter has finally a total

differential error dS expressed in terms of 26 independent complex differentials instead of 22, that is in terms of 104 independent real quantities (52 real parameters and 52 real differential errors) instead of 88 in the case of the SLOdT, that is 16 more (8+8). Thus, the contour of the complex DERs result from 22 orthogonals and 4 circles and have 176 vertices if standard matching

A Non-Zero Length Through

Non-Zero Length could be ei-

ther an adapter/barrel or a

short segment of a transmis-

sion line. Then, T_{11} and T_{22}

have zero value and the L, T,

dL, dT from (4)-(7), are sim-

A Through standard with

Loads are used.

plified as:

$$T = (t_{21} - X)[\Pi (A - B)(a - b)]/(T_{21}EF)$$
(23)

$$dL = \{ \sum (B - C)(b - t_{11})(c - t_{11})[(B - C)(b - a)(c - a)dA - (b - c)(B - A)(C - A)da \} + [\Pi (A - B)(a - b)]dt_{11} \} / (T_{12}T_{21}E^{2}) - dT_{11} / (T_{12}T_{21}) - J^{2}dT_{22} / (T_{12}T_{21}E)^{2} - J(T_{21}dT_{12} + T_{12}dT_{21}) / [(T_{12}T_{21})^{2}E]$$
(24)

$$dT = \{(t_{21} - X)\sum\{(A - B)(C - A)(a - b)(C - a)[B(t_{11} - b) - C(t_{11} - c)]\} - E[F + 2(a - b)B(A - C)]\} \cdot \{[\Pi (a - b)](B - C)^{2}dA - [\Pi (A - B)](b - c)^{2}da\}/(T_{21}F^{2}E^{2}) - [\Pi (A - B)(a - b)]\{(t_{21} - X)[(\sum c(B - A))dt_{11}/(T_{21}FE^{2}) + dT_{21}/((T_{21})^{2}FE) + JdT_{22}/(T_{12}(T_{21})^{2}FE^{2}))] + (dX - dt_{21})/(T_{21}FE)\}$$
(25)

where H from (16) has been transformed to J

 $J = -\sum (ab + ct_{11})(B - A)C$ (26)

(27)

SLOT System Error Differentials and Uncertainties

When the Indirect Through is due to the same type/sex of connectors on both ports then the commonly used Short, matching Load and Open calibration standards will be the same for both SLO one-port calibration, while if different types of connectors are used on the two ports, the standards will be different. Thus, the SLO values are

A = A' = -1

B = B' = 0

C = C' = 1

The next issue is to determine the values T_{ij} of the Non-Zero Length Through standard. Considering it as a transmission line segment of length ℓ , then

$$T_{11} = T_{22} = 0$$
 (28a)

$$T_{12} = T_{21} = e^{-\gamma \ell}$$
 (28b)

where $\gamma = \alpha + i \beta$ is the wellknown complex propagation coefficient. (27) and (28) are substituted in (22)-(25) to produce the following expressions for the corresponding system errors and their differentials

$$L = \frac{e^{2\gamma \ell}(a - c)(b - t_{11})}{[t_{11}(a + c - 2b) + b(a + c) - 2ca]}$$
(29)

$$T = \frac{e^{\gamma \ell}}{2(t_{21} - X)(a - b)(b - c)/[t_{11}(a + c - 2b) + b(a + c) - 2ca]} (30)$$

$$dL = e^{2\gamma\ell} \{ (b - t_{11})(c - t_{11})[(b - a)(c - a)dA + 2(b - c)da] + 2(c - t_{11})(a - t_{11})[2(c - b)(a - b)dB + (c - a)db] + (a - t_{11})(b - t_{11})[(a - c)(b - c)dC + 2(a - b)dc] + 2(a - b)(b - c)(c - a)dt_{11} \} / [t_{11}(a + c - 2b) + b(a + c) - 2ca]^{2} - e^{2\gamma\ell}dT_{11} - e^{4\gamma\ell}(a - c)^{2}(b - t_{11})^{2}dT_{22} / [t_{11}(a + c - 2b) + b(a + c) - 2ca]^{2} + b(a + c) - 2ca]^{2} - e^{2\gamma\ell}(a - c)(b - t_{11})(dT_{12} + dT_{21}) / [t_{11}(a + c - 2b) + b(a + c) - 2ca]$$
(31)

$$dT = e^{\gamma \ell} (t_{21} - X) \{ (c - a)^{2} (b - c) (b - t_{11}) \\ \cdot [(b - a) (c - a) dA + 2(b - c) da] \\ + 2(c - a) [(t_{11} - a) (c - b)^{2} - (c - t_{11}) (a - b)^{2}] \\ \cdot [2(c - b) (a - b) dB + (c - a) db] \\ + (a - b) (b - t_{11}) (a - c)^{2} \\ \cdot [(a - c) (b - c) dC + 2(a - b) dc] \} \\ / [t_{11} (a + c - 2b) + b(a + c) - 2ca]^{2} (c - a)^{2} \\ + e^{\gamma \ell} (t_{21} - X) 2(a - b) (b - c) \{ (2b - a - c) dt_{11} \\ / [t_{11} (a + c - 2b) + b(a + c) - 2ca] - e^{\gamma \ell} dT_{21} \\ - e^{2\gamma \ell} (a - c) (b - t_{11}) dT_{22} - dX + dt_{21} \} \\ / [t_{11} (a + c - 2b) + b(a + c) - 2ca] \qquad (32)$$

The red color in (29)-(32)indicates the additional factors and terms with respect to the Direct Through [1]. This implies that if we consider $T_{12} = T_{21} = 1$ and $dT_{1j} = 0$ then the result expressions will be identical with those for the Direct Through. The remaining SLOT system errors and their differentials have already been expressed in [1]-[4].

For a lossless transmission line in high frequencies $\alpha \ell \approx 0$, $\beta \ell = 2\pi(\ell/\lambda)$ and $\lambda = cv_f$ /f, with c the velocity of (34)

light, v_f the velocity factor and f the frequency. Thus,

 $\beta \ell = 2\pi \ell f[MHz]/(v_{f}300)$ (33)

vℓ≈iβℓ

and from (28b)

 $T_{12} = T_{21} = e^{-i\beta\ell}$ (35)

The L, T, L', T' system errors are shown in Fig. 3 against frequency for the Direct Through and in Fig. 4 for the Indirect Through. Tab. 2 contains the standard loads uncertainties that were adopted for the present results, based on available manufacturer's data [3], [5]-[7]. Since T_{11} and T_{22} have nominal value zero their uncertainties dT_{11} and dT_{22} are represented by circular DERs with radius to be determined from the return loss (or SWR) specifications. On the other hand dT_{12} and dT_{21} are rectangular DERs. For their magnitude and phase uncertainties the specifications for insertion loss and electrical length were used from the most relevant reference since

there were no available such data for the used Through. The length uncertainty is consistent with the mechanical tolerance. As measurement inaccuracies the ±1 digit in LSD for magnitude and phase was assumed as in [1]-[4].

Fig. 5 shows the L-DERs and DEIs at the frequency of 639 [MHz] where ZT stands for the Zero Length Through case (black), NZT for the Non-Zero Length Through case (blue), while the red colored DER corresponds to the NZT but without (w/o) take into account the Through standard in calculations and the green colored DER to the NZT but without the dT_{ii} terms. The T-DERs and DEIs are shown in Fig. 6 using the same notations. Although the L-DERs intersect in large areas the same is not true for T-DERs where in each case the corresponding differential error region (and intervals) is in a different scale, resulting in an impossible direct comparison as shown in Fig. 7(a). Thus, the regions are given in separate figures (b, c and d) from which their totally different shapes are depicted.

Tab. 2: Standard Loads Uncertainty

A, C		В	T ₁₁ , T ₂₂	T ₁₂ , T ₂₁		
-0.01, 0	±2°	0.029	0.025	±0.08[dB]	±0.0002[m]	



v1–18

FUNKTECHNIKPLUS # JOURNAL



Fig. 5: L-DERs at 639 [MHz]

Results

The two-port DUT is shown



Fig. 6: T-DERs at 639 [MHz]

in Fig. 7. It is a simple Tresistive network with input impedance far from 50 Ohms for both ports, with horizontal arms $Z_1 = 24.2 [\Omega], Z_2 =$ 120 [Ω] and vertical arm $Z_{12} =$

1.1 [Ω]. This box was constructed with female connector at both ports, and a female to female adapter served as the through standard for the SLOT calibration. Then the connector of port 1 was changed to male and the SLOdT calibration method was applied [1], [2]. The VNA system used was described in [1] and the measurements were made from 2 to 1289 [MHz].



Fig. 7: The T-Resistive box in situ

The typical details for the Type-N connectors, and especially those for the reference plane were taken initially by [8]. A figure for both sexes with all the dimensions is illustrated there and there is also an indication of a plus/minus mechanical tolerance.

After a careful measurement of the real dimensions of the used adapter with a digital vernier caliper and from its specifications [5], its length ℓ was determined from its physical length of 47.48 [mm] and the reference plane of the female connectors, as

$\ell = 47.48 - 2 \cdot 9 = 29.48$ [mm]

The adapter was then considered as a small segment of lossless transmission line with return loss 32 [dB] for its two ports (specifications before 2007). This piece of line can be considered as an "almost short" Through connection as it is equal to about one-tenth of a wavelength at the frequency, for example, of 1 [GHz] and not to one-hundredth as it is mentioned in [9]. Actually, it varies between 0.2 to 13 hundredths in the whole measured frequency range.

Fig. 8 shows analytically the measurements of S₂₁ DUT parameter. At (8a) the black colored curve corresponds to the measurement of S_{21} with SLOdT (ZT: Zero Length Thru) and the red color curve to the measurements of S_{21} with a Non-Zero Length Through but without (w/o) take it into account in calculations (NZT: Non-Zero Length Thru). It is obvious, how the presence of the Through standard affected the measurements. At (8b) the green color curve corresponds to the measurements of S_{21} with Non-Zero Length Through but now, we do consider it, having an electrical length at 1 [GHz]. Below at (8c) the magenta color curve resulted for the Through with an electrical length at the central frequency of 639 [MHz] and at (8d) the blue colored curve for the Through with electrical length as function of frequency.

The middle frequency was selected since it is important for the determination of the reference plane if the TRL calibration will be applied while the 1 [GHz] was selected as a characteristic frequency, both for comparison reasons [9], [10].

It is essential that the most accurate measurement of SLOdT with the Direct Through connection was used as reference, that is, the black curve, and the conclusion was that a Non-Zero Length Through must be considered as frequency dependent.

In Fig. 9 all the four S parameters are shown. The four above mentioned cases are examined for the Through measurements both for Direct and Indirect connection for each S parameter. It is evident, how the presence of the Through standard affected the measurements.



v1–21





Obviously there is a very small change at S_{11} and S_{22} measurements, but the Through influence can not be omitted at S_{12} and S_{21} .

To illustrate the DERs for the four S parameters of the DUT the three most important cases have been chosen to be included: (i) the SLOdT results in black color, (ii) the Non-Zero Through is used but it is neglected, in red color, and (iii) the results from the full expressions for the differential errors when SLOT calibration is performed with a Non-Zero Length Through between the two ports which is not neglected, in blue color.

Fig. 10 shows the S₁₁ parameter. A number of selected S-DER frames are drawn explicitly. At the last right figure we tried to give a comparison of these cases, which is rather difficult in the complex plane.

The shape of the DERs in Fig. 10 is different and variable with frequency. But since this is the S_{11} parameter we can see that DERs are overlapping almost for the entire frequency range for

all the three cases

In Fig. 11 S_{21} parameter is given. The differences here are clearer. Obviously, the DERs of the SLOT case (blue color) are larger from those of SLOdT, as it was expected since four more uncertainties have been added. The same is true for the S_{12} parameter in Fig. 12.



Fig. 10: S₁₁-DER with SLOdT and SLOT





The figures with the measurement results for S_{21} and S_{12} are almost overlapping, and the reciprocity is approximately satisfied for the DUT. A simple way to visualize that fact is to move back and forward between the two figures.

At Fig. 13 the S_{22} -DERs are shown. From the last right figure (d) it is obvi-

ous that there is almost none effect at the S_{22} by considering or not the influence of Non-Zero Length Through.

Fig. 14 shows the S_{11} -DERs for the three examined cases at the central frequency. The rectangular Differential Error Intervals [DEIs] (Real and Imaginary) and the polar DEIs (magnitude and phase) are included.



Fig. 12: S₁₂-DER with SLOdT and SLOT

The black DER in Fig. 14 (Direct Through), has a contour of 160 points, while the blue DER (Indirect Through) has a contour of 176 points. At this frequency, the DER for the case of not taking into account the presence of the Through (red color), is indeed much larger. It is worth to notice that S_{11} with the Non-Zero Length Through

standard, blue point, is inside the black DER. A green colored DER that is slightly smaller than the blue DER of non-zero Through case, and hardly shown in the figure is the one that results from the full expressions for the Non-Zero Length Through but by considering that differential errors dT_{11} , dT_{22} are zero.





In Fig. 15 the S_{21} -DERs with the corresponding Rectangular and Polar DEIs, are shown. The blue S_{21} point that corresponds to the Non-Zero Length Through measurements is again inside the black DER from the Zero Length Through case. Obviously there is an overlapping of these two DERs. The green DER is now well shown. Since Figs. 14 and 15 are already too complicated, Tab. 3 contains the magnitude in [dB] and the phase in [°] of S_{11} and S_{21} in 639 [MHz] for the four illustrated polar DEIs with the corresponding signed maximum values (positive and negative, not symmetrical in general) of the estimated uncertainties.



Tab. 3: Positive and Negative Maximum Uncertainty

S ₁₁									
	Magnitude [dB]			Phase [°]					
	Value	-	+	Value	-	+			
ZT	-1.408	0.393	0.481	-10.75	4.87	5.00			
NZT-w/o	-1.063	0.627	0.754	-6.52	7.73	7.88			
NZT-dT _{ii}	-1.063	0.149	0.270	-6.53	4.81	4.83			
NZT	-1.063	0.153	0.274	-6.53	4.84	4.85			
S ₂₁									
ZT	-18.067	0.668	0.632	-44.23	5.71	5.80			
NZT-w/o	-18.174	0.634	0.599	-17.44	5.22	5.19			
NZT-dT _{ii}	-18.023	1.089	0.951	-40.85	6.53	6.81			
NZT	-18.023	1.231	1.062	-40.85	7.35	7.64			

v1–27

Conclusion

The most complex case of the full two-port calibration when a Non-Zero Length standard as Through connection is required was examined analytically. The most complicated expressions where simplified and applied in the case of SLOT calibration on a simple T-resistive network.

In contrast with SLO standards, the parameters value of an Indirect Through is frequency depended and its influence cannot be neglected especially for the transmission scattering parameters.

References

[1] Yannopoulou N., Zimourtopoulos P., "S-Parameter Uncertainties in Network Analyzer Measurements with Application to Antenna Patterns" Radioengineering, Vol. 17, No. 1, April 2008, pp. 1-8

www.radioeng.cz/fulltexts/2008/08_01_01_08.pdf

- [2] Yannopoulou N.I., Zimourtopoulos P.I., "Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 2: Full Two-Port Calibration", FunkTechnikPlus # Journal, Issue 1, Year 1, 2013, pp. 23-30 www.otoiser.org/index.php/ftpj/article/view/43/38
- [3] Yannopoulou N., Zimourtopoulos P., "Total Differential Errors in One Port Network Analyzer Measurements with Application to Antenna Impedance", Radioengineering, Vol. 16, No. 2, June 2007, pp. 1-8 www.radioeng.cz/fulltexts/2007/07_02_01_08.pdf
- [4] Yannopoulou N.I., Zimourtopoulos P.E., "Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 1: Full One-Port Calibration", FunkTechnikPlus # Journal, Issue 1, Year 1, October 2013, pp.17-22

www.otoiser.org/index.php/ftpj/article/view/42/37

- [5] Agilent (HP), "HP 1250-1472 Adapter Type-N (f) to Type-N (f) specifications"
- [6] Hiebel M., "Fundamentals of Vector Network Analysis", Rohde & Schwarz, Ed. 5th, Ch 3, §3.3.1, p.97 www.books.rohde-schwarz.com/go/rohdeschwarz/_ws/resource /_ts_1394853419000/r00ABXQAG3N0YXRfcHJpdjpwcm9kdWN0czpta F9mb3ZuYQ==/data_info/nwa_e_lp.pdf

- [8] Laverghetta T.S., "Microwave Measurements and Techniques", Artech House, 1976, p.78
- [9] Agilent Application Note 1291-1B, "10 Hints for Making Better Network Analyzer Measurements", Agilent Technologies, Inc., October, 2001
- [10]Agilent Application Note AN 1287-9, "In-Fixture Measurements Using Vector Network Analyzers ", Agilent Technologies, 2000
 - *Active Links: 19.09.2016 Inactive Links : FTP#J Link Updates: http://updates.ftpj.otoiser.org/

Previous Publication in FUNKTECHNIKPLUS # JOURNAL

"[tlnomiva] : Transmission Line Nominal Values without Tolerance - from Cable Specifications and Technical Data Sheets : FLOSS for MS Windows", Issue 10, Year 3, pp. 7 - 36

* About The Authors

Nikolitsa Yannopoulou, Issue 9, Year 3, p. 390

yin@arg.op4.eu

Petros Zimourtopoulos, Issue 9, Year 3, p. 390 pez@arg.op4.eu In case of any doubt, download the genuine papers from genuine.ftpj.otoiser.org

[This Page Intentionally Left Blank]

This paper is licensed under a Creative Commons Attribution 4.0 International License — <u>https://creativecommons.org/licenses/by/4.0/</u>

FRONT COVER VIGNETTE

A faded synthesis of an anthemion rooted in a meandros

The thirteen-leaf is a symbol for a life tree leaf. "Herakles and Kerberos", ca. 530–500 BC, by Paseas, the Kerberos Painter, Museum of Fine Arts, Boston.

www.mfa.org/collections/object/plate-153852

The simple meandros is a symbol for eternal immortality. "Warrior with a phiale", ca. 480—460 BC, by Berliner Maler, Museo Archeologico Regionale "Antonio Salinas" di Palermo.

commons.wikimedia.org/wiki/File:Warrior_MAR_Palermo_NI2134.jpg

FUNKTECHNIKPLUS # JOURNAL e4-32 ISSUE 11 - YEAR 4

ARG NFP AOI

Antennas Research Group Not-for-Profit Association of Individuals [*] www.arg.op4.eu – arg@op4.eu Hauptstraße 52, 2831 Scheiblingkirchen, Austria Telephone: 0 6646311483 – International: 0043 6646311483 * The Constitution of Greece, Article 12(3) – 2008: www.hellenicparliament.gr/en/Vouli-ton-Ellinon/To-Politevma * The Hellenic Supreme Court of Civil and Penal Law: www.areiospagos.gr/en – Court Rulings:Civil|A1|511|2008